Solution

Part 1a

a.
$$v_{ret} = \sqrt{v_0^2 - 2(e/m)V} = 1.956 \times 10^6 \, m/s$$

$$v_{acc} = \sqrt{v_0^2 + 2(e/m)V} = 2.044 \times 10^6 \, m/s$$
(0.5 pts)

$$x_{ret} = v_{ret}t$$
, $x_{acc} = v_{acc}(t - T/2)$ (0.5 pts)

$$x_{ret} = x_{acc}$$
 \rightarrow $t_{bunch} = \frac{v_{acc}T}{2(v_{acc} - v_{ret})} = 11.61T$ (0.3 pts)

$$b = v_{ret} t_{bunch} = 2.272 \times 10^{-2} m.$$
 (0.2 pts)

b. The phase difference:

$$\Delta \varphi = \pm (\frac{t_{bunch}}{T} - n)2\pi = \pm 0.61 \times 2\pi = \pm 220^{\circ}.$$
 (1.0 pts)

OR
$$\Delta \varphi = \pm 140^{\circ}$$

Part 1b

$$\rho_L = n_L \frac{M}{N_A} \tag{0.3 pts}$$

where $n_{\!\scriptscriptstyle L}$ is the number of molecules per cubic meter in the liquid phase

Average distance between the molecules of water in the liquid phase:

$$d_L = (n_L)^{-\frac{1}{3}} = (\frac{M}{\rho_L N_A})^{\frac{1}{3}}$$
 (0.2 pts)

P_aV=nRT

where n is the number of moles (0.6 pts)

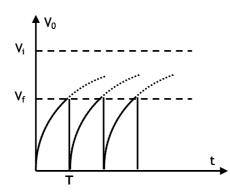
$$P_a = \frac{nM}{V}\frac{RT}{M} = \rho_V\,\frac{RT}{M} = \frac{n_VM}{N_A}\frac{RT}{M}$$

where n_V is the number of molecules per cubic meter in the vapor phase. (0.9 pts)

$$d_V = (n_V)^{-1/3} = (\frac{RT}{P_a N_A})^{\frac{1}{3}}$$
 (0.2 pts)

$$\frac{d_V}{d_L} = (\frac{RT\rho_L}{P_o M})^{\frac{1}{3}} = 12$$
 (0.3 pts)

a. (0.5 pts.)



b.
$$V_i >> V_f$$
 (0.2 pts)
c. $V_f = V_i \left(1 - e^{-T/RC}\right)$ (0.2 pts)

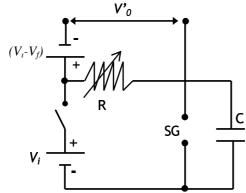
 $e^{-T/RC} \approx 1 - (T/RC)$ T/RC<<1,

then

$$T = (V_f / V_i) RC$$
 (0.2 pts)

(0.2 pts) (0.2 pts) (0.4 pts)

d. Re. SG and Rf. Correct circuit



$$V_0^{'}$$
 (0.3 pts) $V_i^{'} - V_f$ with the correct polarity (0.3 pts)

$$V_i' - V_f$$
 with the correct polarity (0.3 pts)

Total (1.0 pts)

Part 1d

As the beam passes through a hole of diameter D the resulting uncertainty in the y-component of the momentum;

$$\Delta p_y \approx \frac{\hbar}{D}$$
 (0.6 pts)

and the corresponding velocity component;

$$\Delta v_y \approx \frac{\hbar}{MD}$$
 (0.4 pts)

Diameter of the beam grows larger than the diameter of the hole by an amount

$$\Delta D = \Delta v_y$$
.t , where t is the time of travel. (0.2 pts)

If the oven temperature is T, a typical atom leaves the hole with kinetic energy

$$KE = \frac{1}{2}Mv^2 = \frac{3}{2}kT$$
 (0.4 pts)

$$v = \sqrt{\frac{3kT}{M}}$$
 (0.2 pts)

Beam travels the horizontal distance L at speed v in time

$$t = \frac{L}{v}$$
, so (0.2 pts)

$$\Delta D = t\Delta v_y \approx \frac{L}{v} \frac{\hbar}{MD} = \frac{L\hbar}{MD\sqrt{\frac{3kT}{M}}} = \frac{L\hbar}{D\sqrt{3MkT}}$$
 (0.4 pts)

Hence the new diameter after a distance L will be;

$$D_{\text{new}} = D + \frac{L\hbar}{D\sqrt{3MkT}}$$
 (0.1 pts)