

The net work done by 1 mol of the gas is

$$W = \frac{R}{\kappa - 1}(T_1 - T_2) + \frac{R}{\kappa - 1}(T_3 - T_4) = \frac{R}{\kappa - 1}(T_1 - T_2 + T_3 - T_4)$$

and the heat supplied to the gas is

$$Q_{23} = C_V(T_3 - T_2).$$

Hence, we have for thermal efficiency

$$\eta = \frac{W}{Q_{23}} = \frac{R}{(\kappa - 1)C_V} \frac{T_1 - T_2 + T_3 - T_4}{T_3 - T_2}.$$

Since

$$\frac{R}{(\kappa - 1)C_V} = \frac{C_p - C_V}{(\kappa - 1)C_V} = \frac{\kappa - 1}{\kappa - 1} = 1,$$

we obtain

$$\eta = 1 - \frac{T_4 - T_1}{T_3 - T_2} = 1 - \frac{T_1}{T_2} = 1 - \varepsilon^{1-\kappa}.$$

Numerically,  $\eta = 1 - 300/738 = 1 - 0.407$ ,  $\eta = 59,3\%$ .

d) Actually, the real  $pV$ -diagram of the cycle is smooth, without the sharp angles. Since the gas is not ideal, the real efficiency would be lower than the calculated one.

**Problem 2.** Dipping the frame in a soap solution, the soap forms a rectangle film of length  $b$  and height  $h$ . White light falls on the film at an angle  $\alpha$  (measured with respect to the normal direction). The reflected light displays a green color of wavelength  $\lambda_0$ .

- a) Find out if it is possible to determine the mass of the soap film using the laboratory scales which has calibration accuracy of 0.1 mg.
- b) What color does the thinnest possible soap film display being seen from the perpendicular direction? Derive the related equations.

Constants and given data: relative refractive index  $n = 1.33$ , the wavelength of the reflected green light  $\lambda_0 = 500$  nm,  $\alpha = 30^\circ$ ,  $b = 0.020$  m,  $h = 0.030$  m, density  $\rho = 1000$  kg m<sup>-3</sup>.