

Solution

We can not rely on any value about the density of the glass. It is quite uncertain. The index of refraction can be determined using a light beam which does not touch the bubble. Another method consists of immersing the sphere into a liquid of same refraction index: its surface becomes invisible.

A great number of methods can be found.

We can start by determining the axis, the line which joins the centers of the sphere and the bubble. The easiest way is to use the “tumbler-over” method. If the sphere is placed on a horizontal plane the axis takes up a vertical position. The image of the bubble, seen from both directions along the axis, is a circle.

If the sphere is immersed in a liquid of same index of refraction the spherical bubble is practically inside a parallel plate (Fig. 11). Its boundaries can be determined either by a micrometer or using parallel light beams.

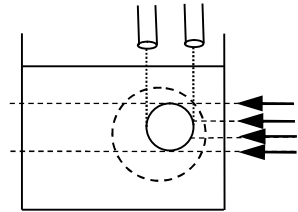


Figure 11

Along the axis we have a lens system consisting of two thick negative lenses. The diameter of the bubble can be determined by several measurements and complicated calculations.

If the index of refraction of the glass is known we can fit a plano-concave lens of same index of refraction to the sphere at the end of the axis (Fig. 12). As ABCD forms a parallel plate the diameter of the bubble can be measured using parallel light beams.

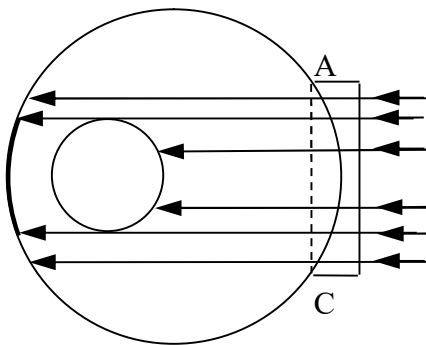


Figure 12

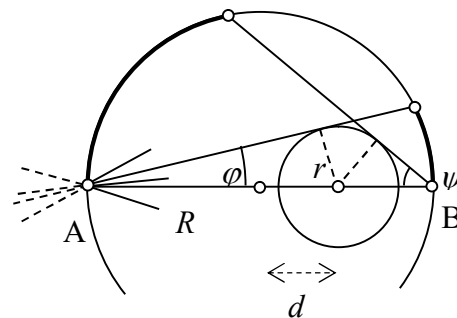


Figure 13

Focusing a light beam on point A of the surface of the sphere (Fig. 13) we get a diverging beam from point A inside the sphere. The rays strike the surface at the other side and illuminate a cap. Measuring the spherical cap we get angle φ . Angle ψ can be obtained in a similar way at point B. From

$$\sin \varphi = \frac{r}{R+d} \quad \text{and} \quad \sin \psi = \frac{r}{R-d}$$

we have

$$r = 2R \cdot \frac{\sin \psi \sin \varphi}{\sin \psi + \sin \varphi}, \quad d = R \cdot \frac{\sin \psi - \sin \varphi}{\sin \psi + \sin \varphi}.$$

The diameter of the bubble can be determined also by the help of X-rays. X-rays are not refracted by glass. They will cast shadows indicating the structure of the body, in our case the position and diameter of the bubble.

We can also determine the moment of inertia with respect to the axis and thus the diameter of the bubble.

Experimental problem

The whole text given to the students:

At the workplace there are beyond other devices a test tube with 12 V electrical heating, a liquid with known specific heat ($c_0 = 2.1 \text{ J/g}^\circ\text{C}$) and an X material with unknown thermal properties. The X material is insoluble in the liquid.

Examine the thermal properties of the X crystal material between room temperature and 70°C . Determine the thermal data of the X material. Tabulate and plot the measured data.

(You can use only the devices and materials prepared on the table. The damaged devices and the used up materials are not replaceable.)

Solution

Heating first the liquid then the liquid and the crystalline substance together two time-temperature graphs can be plotted. From the graphs specific heat, melting point and heat of fusion can be easily obtained.

Literature

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