Problems of the 9th International Physics Olympiads (Budapest, Hungary, 1976)

Theoretical problems

Problem 1

A hollow sphere of radius R = 0.5 m rotates about a vertical axis through its centre with an angular velocity of $\omega = 5 \text{ s}^{-1}$. Inside the sphere a small block is moving together with the sphere at the height of R/2 (Fig. 6). ($g = 10 \text{ m/s}^2$.)

- a) What should be at least the coefficient of friction to fulfill this condition?
- b) Find the minimal coefficient of friction also for the case of $\omega = 8 \text{ s}^{-1}$.
- c) Investigate the problem of stability in both cases,
 - α) for a small change of the position of the block,
 - β) for a small change of the angular velocity of the sphere.

